

# Brout-Englert-Higgs monopoles: particlelike solutions in modified gravity

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FFP14 - July 17, 2014

*Particlelike distributions of the Higgs field nonminimally coupled to gravity,*  
**A. Füzfa, M. Rinaldi, S.S., PRL 111 (2013) 121103**

*Particlelike solutions of modified gravity: the Higgs monopoles,*  
**S.S., M. Rinaldi, F. Staelens, A. Füzfa,**  
*arXiv:1405.5476 (accepted by PRD)*



# Motivations

- General relativity (GR) and the Standard Model cannot explain (satisfactorily)
  - Current cosmic acceleration without coincidence issues
  - Dark matter effects
  - Flatness and horizon problems (**primordial inflation**)

... but never been faulted by observations/experiments as well !

—→ Modified gravity (**scalar-tensor theory**,  $F(R)$ , massive gravity, extra dimensions...)?

- Constraints on deviations from GR
  - Solar-system constraints (e.g. Cassini probe)
  - Astrophysical tests (e.g. binary pulsar)
  - Experimental tests (e.g. torsion balance)

# BEH field, partner of the metric?

- Why the BEH field?
  - Only fundamental scalar field detected (up to now)
  - Elementary particles mass generation
  - Partner to gravity?
- Some simplifications
  - Unitary gauge

$$\phi(x) = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}$$

- Coupling between the BEH field to matter in modified gravity not considered so far

*Greenwood, Kaiser, Sfakianakis, PRD 87 (2013): 064021*

*Rinaldi, Eur.Phys.J.Plus (2014) 129: 56*

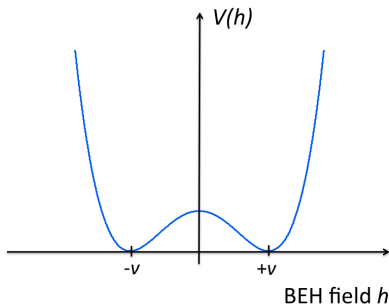
# (New) Higgs inflation

*The Standard Model Higgs boson as the inflaton,  
Phys. Lett. B 659 (2008) 703,  
F. L. Bezrukov and M. Shaposhnikov*

# Viable inflation?

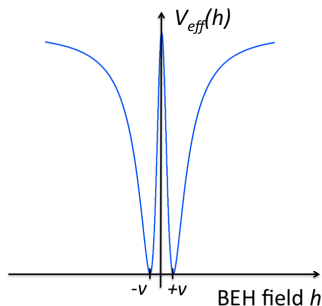
Very early model ('80):  
"minimally coupled BEH field"

$$\mathcal{L} = \frac{m_{pl}^2}{16\pi} R - \frac{1}{2} (\partial\phi)^2 - V(\phi)$$



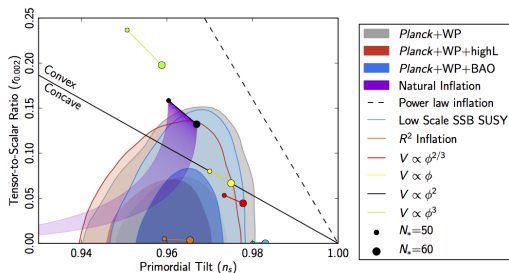
New Higgs inflation (2008):  
"non-minimally coupled BEH field"

$$\mathcal{L} = \frac{m_{pl}^2}{16\pi} (1 + \xi\phi^2) R - \frac{1}{2} (\partial\phi)^2 - V(\phi)$$

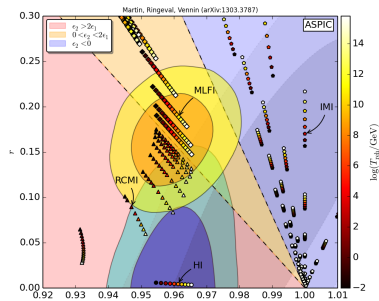


# New Higgs inflation, a viable model?

- Constraint: Non-minimal coupling  $\xi > 10^4$
- At high energy: equivalent to  $R^2$  inflation
- Favoured by Planck data
- Ruled out by BICEP 2 results (no tensor modes)



Planck 2013 results.  
XXII. Constraints on inflation



J. Martin, C. Ringeval, V. Venin  
arXiv:1303.3787



# Higgs monopoles

# Introduction

- Solutions in static spherically symmetric spacetime

$$\mathcal{L} = \frac{m_{pl}^2}{16\pi} \left( 1 + \frac{\xi}{m_{pl}^2} H^2 \right) R - \frac{1}{2} (\partial H)^2 - V(H) + \mathcal{L}_{mat} [\Psi_m, g_{\mu\nu}]$$

$$\text{with } H = m_{pl} h \tilde{v}, \quad \tilde{v} = 246 \text{ GeV} / m_{pl}$$

$$V(H) = \frac{\lambda}{4} (H^2 - v^2)^2$$

- Standard Model potential parameters
- Matter = top-hat density profile
- **Distribution of the BEH field around compact objects?**
- **Deviations from GR?**



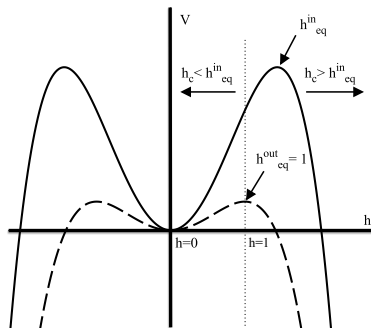
# Effective dynamics

- Klein-Gordon equation  $\square h = -\frac{dV_{\text{eff}}}{dh}$   
with  $V_{\text{eff}} = -V + \frac{\xi h^2 R}{16\pi}$
- In cosmology (FLRW metric, scale factor  $a(t)$ )

$$\frac{d^2 h}{dt^2} + \frac{3}{a} \frac{da}{dt} \frac{dh}{dt} = \frac{dV_{\text{eff}}}{dh}$$

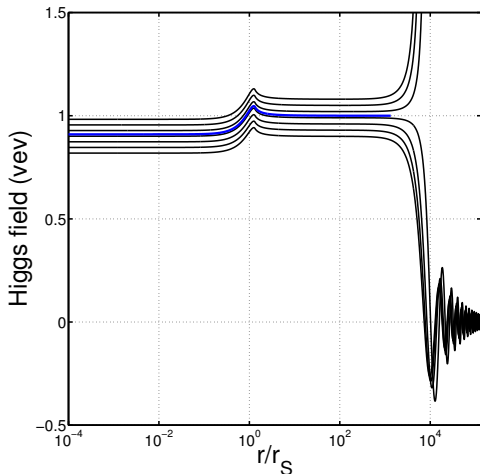
- For compact objects (Schwarzschild coordinates)

$$h'' - h' \left( \lambda' - \nu' - \frac{2}{r} \right) = -\frac{dV_{\text{eff}}}{dh}$$



# Higgs monopole solutions

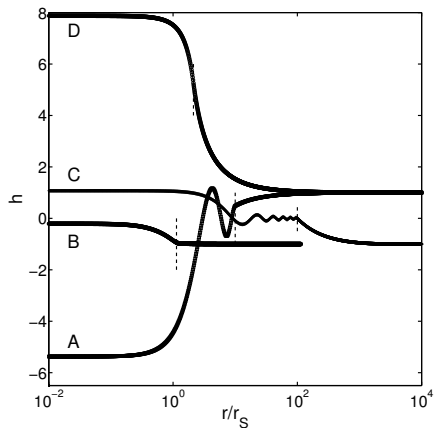
$$\xi = 10, m = 10^6 \text{ kg}, s = 0.75$$



- Particlelike solutions:
  - Convergence towards the vev
  - Globally regular
  - Finite energy
  - Asymptotically flat
- In GR, unrealistic homogeneous solution only ( $h = 1$  everywhere)
- Parameters
  - Compactness  $s = \frac{r_S}{\mathcal{R}}$  with  $r_S$ , the Schwarzschild radius and  $\mathcal{R}$ , the radius
  - Baryonic mass  $m$
  - Non-minimal coupling  $\xi$



# Monopole family



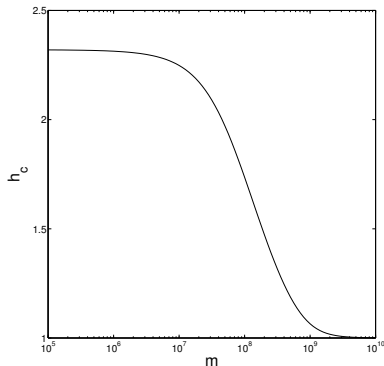
	$h_c$	$\xi$	$m$	$s$
A	- 5.37	$10^4$	$10^3$ kg	0.1
B	- 0.21	10	$10^6$ kg	0.88
C	1.077	$10^6$	$10^6$ kg	0.01
D	7.88	60	$10^4$ kg	0.47

Notice: no astrophysical objects

# Deviations from GR

- Astrophysical objects:  
 $h_c \rightarrow 1$
  - No observable deviations from GR with SM potential parameters
  - Even for big values of  $\xi$
  - Vev vs Planck scale ("hierarchy problem")
- 
- **Only one solution, different than GR !**

$\xi = 60, s = 0.2$  (neutron star)

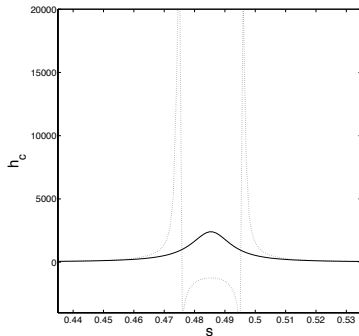
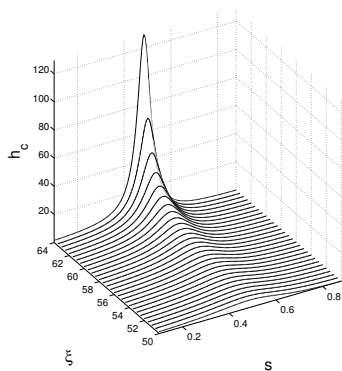


# Amplification mechanism (I)

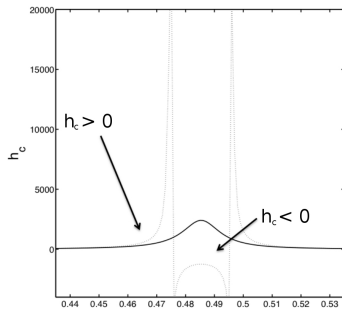
$$m = 10^3 \text{ kg}$$

$\xi = 64.6$  (solid line)

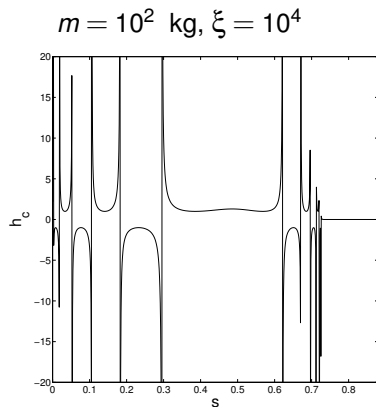
$\xi = 64.7$  (dotted line)



# Amplification mechanism (II)



- Critical  $\xi$ :  $h_c \rightarrow \infty$  for some  $s$  (or  $\mathcal{R}$ )
- Phase transition  $h_\infty \rightarrow \pm 1$
- Constraint on  $\xi$ : forbidden  $s$  (or  $\mathcal{R}$ )  
 $\rightarrow$  No (monopole) solution !



# Conclusions and perspectives

## Conclusion:

- New particlelike solution: Higgs monopole
- Different than GR and usual scalar-tensor theory (no potential)
- Negligible deviations from GR (SM potential parameters)
- General amplification mechanism

## Perspectives:

- Coupling BEH field to matter (cosmology and compact objects)
- Unitary gauge
- Possible formation during gravitational collapse and stability? Remnants?
- Generalization of amplification mechanism (other potential)
- Application to boson stars